

補充資料 I (Regular Grammar)

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Grammar Definition

$G=(V,T,S,P)$, where

V : a finite set of **variables**(**Non-terminal**)

T : a finite set of **terminal** symbols(**terminal**)

$S \in V$ is a special symbol called **start variable**

P is a finite set of **productions**(**rules**)

Example

$G = (\{S\}, \{a,b\}, S, P)$, where P are given by

$S \rightarrow aSb \mid \lambda$ (recursive grammar rule)

\mid is logical OR for production.

Derivation processes:

$S \Rightarrow aSb \Rightarrow aaSbb \Rightarrow aabb$

Grammar produces a language result:

$$L(G) = \{ a^n b^n : n \geq 0 \}$$

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Example

$G = (\{S,A\}, \{a,b\}, S, P)$, where P are given by

$S \rightarrow Ab$

$A \rightarrow aAb \mid \lambda$

Grammar produces a language result:

$$L(G) = \{ a^n b^{n+1} : n \geq 0 \}$$

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Example

$G = (\{S\}, \{a, b\}, S, P)$, where P are given by
 $S \rightarrow SS \mid \lambda \mid aSb \mid bSa$

Grammar produces a language result:

$$L(G) = \{ w : n_a(w) = n_b(w) \}$$

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Example

$G = (\{S, A\}, \{a, b\}, S, P)$, where P are given by

$S \rightarrow aAb$

$A \rightarrow aAb \mid \lambda$

Grammar produces a language result:

$$L(G) = \{ a^n b^n : n > 0 \}$$

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DFA Definition(Regular Grammar)

$M=(Q, \Sigma, \delta, q_0, F)$ where

Q : a finite set of **internal states**

Σ : a finite set of **input alphabets**

$\delta : Q * \Sigma \rightarrow Q$ is a **transition function**

$q_0 \in Q$ is the **initial state**

$F \subseteq Q$ is a set of **finite states**

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DFA Example

$M=({q_0, q_1, q_2}, \{0, 1\}, \delta, q_0, \{q_1\})$

Where δ is given by

$\delta(q_0, 0)=q_0$, $\delta(q_0, 1)=q_1$,

$\delta(q_1, 0)=q_0$, $\delta(q_1, 1)=q_2$,

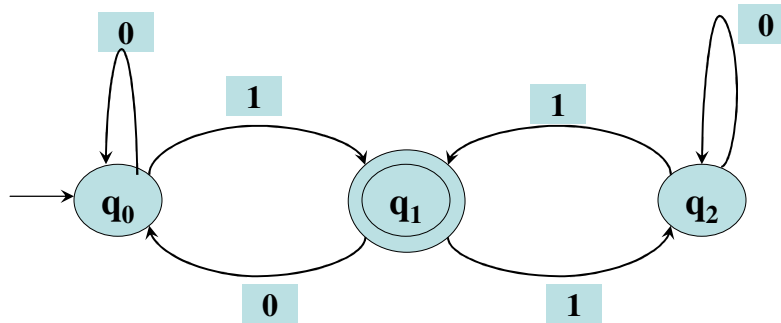
$\delta(q_2, 0)=q_2$, $\delta(q_2, 1)=q_1$,

Input symbol \ Current State	0	1
q_0	q_0	q_1
q_1	q_0	q_2
q_2	q_2	q_1

DFA produces a language result:

$L(\text{DFA})=\{ \text{accept the string } \mathbf{001}(\text{奇數個}1\text{結尾}) \}$

DFA Example(continued)



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DFA Program Example

```
....  
switch (state) {  
  Case 0: ....  
    if (ch == '1') state=1; break;  
  Case 1: ...  
    if (ch == '0') state=0; break;  
}  
.....
```

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<pre>#include <stdio.h> void main() { int state=0; char c; clrscr(); while ((c=getchar()) != '\n') { switch (state) { case 0: switch (c) { case '0': state=0; break; case '1': state=1; break; } break; </pre>	<pre>case 1: switch (c) { case '0': state=0; break; case '1': state=2; break; } break; case 2: switch (c) { case '0': state=2; break; case '1': state=1; break; } break; }</pre>	<pre>printf("%c stat=%d\n", c,state); } if (state == 1) printf(" --> this string is accept by this DFA\n"); else printf(" --> this string is not accept by this DFA\n"); }</pre>
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DFA and Regular Grammar Example

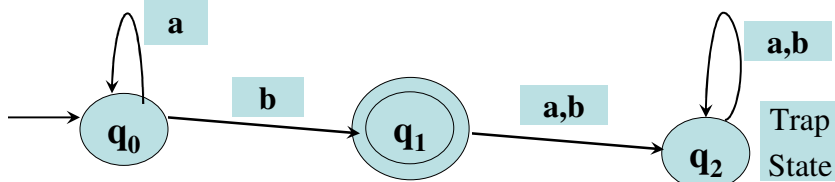
$G = (\{S, A\}, \{a, b\}, S, P)$, where P are given by

$S \rightarrow Ab$

$A \rightarrow aA \mid \lambda$

Grammar produces a language result:

$$L(G) = \{ a^n b : n \geq 0 \}$$



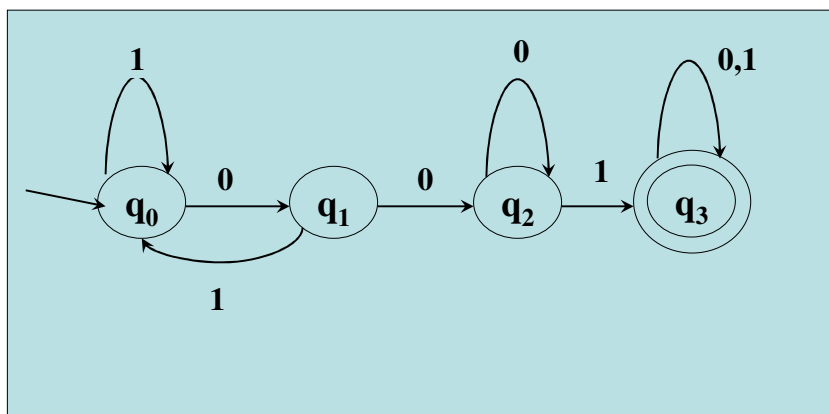
DFA and CFG Example(continue)

Input symbol \ Current State	a	b
q_0	q_0	q_1
q_1	q_2	q_2
q_2	q_2	q_2

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DFA and CFG Example

Find a DFA accept all strings on $\{0,1\}$ containing the **substring 001** ?



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```

accept=0;
while ((c=na[i++]) != '\0') {
    switch (state) {
        case 0: if (c == '0') state=1;    break;
        case 1: if (c == '1') state=0;    if (c == '0') state=2;    break;
        case 2: if (c == '1') state=3;    break;
        case 3: accept=1;    break;
    }
}
if (accept == 0) printf("%s is not accept for substring 001\n",na);
else printf("%s is accept for substring 001\n",na);

```

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DFA and CFG Example

Find a DFA, 判斷一運算式的對錯?
 (以 = 為 final state) [至少需? 個states]
 Ex. $12 + 23 - 45 * 67 =$
 $67 =$ 視為error!!!

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