

# Data mining, machine learning, and uncertainty reasoning

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## 課程進行

- 期中考(20%)、期末考(30%)
- 出席率(10%)
- 報告(40%)

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## Application

- Support the DSS (Decision Supporting System) for reasoning ***business intelligent*** (企業智慧)
  - **Call center** data analysis and assessment
    - Inbound call analysis → for customer service
    - Outbound call analysis → for promotion sale or investigation
  - **Shopping center** data collection and assessment
    - Shopping DM guide → product location reference
    - Shopping habit → customization shopping eDM
  - Support the **ERP system** for constructing better control of enterprise's resource → purchase reference

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## Background Knowledge

- Database
- Data warehouse
- Conditional Probability → Bayesian Theorem

$$P(H | E, c) = \frac{P(H | c) P(E | H, c)}{P(E | c)}$$

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## Relative Topic

- AI or Neural Network
- Database or DataWarehouse
- Data Mining or data reasoning
- Machine learning

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## Concept

Program = algorithm + data

+ **domain knowledge**

Applied **domain knowledge** in suitable **data structure** is fundamental for solving problems.

**Uncertainty propagation** will happen in many expert Systems.

Chess playing game uses **brute-force approach** has led more powerful than **AI method** because **encoding abstract rule** into computer is very difficult.

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## Data Mining

Different perspectives of data mining

- Statistics
- Pattern recognition (**mining data as patterns**)
- Database management system
- Artificial intelligent (**encode domain knowledge into abstract rules**)

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## Relation

- Data mining is first to mine data from a set of databases (**data warehouse**)
- Data that are mined is just **number** which have no meaning to some users → decision making?
- Data can be filtered by machine learning to eliminate some unused data by some **machine learning methods**
- The data left by the machine learning is needed by users which should be supported by some **experts' rules encoding → uncertainty reasoning**

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## Uncertainty reasoning

- Vagueness
- Incompleteness (**imperfect data dealing**)
- Missing value
- Inconsistency

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## What is Learning?

- "Learning denotes **changes** in a system that ... **enable a system to do the same task more efficiently the next time.**" --Herbert Simon
- "Learning is **constructing or modifying representations of what is being experienced.**" --Ryszard Michalski
- "Learning is **making useful changes** in our minds." --Marvin Minsky

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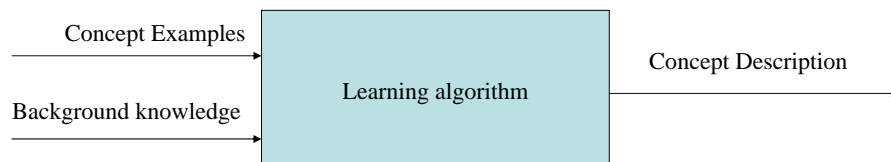
## Why do Machine Learning?

- Understand and improve **efficiency of human learning**  
For example, use to improve methods for teaching and tutoring people, as done in Computer-aided instruction (**CAI**)
- Discover new things or structure that is unknown to humans. Example: **Data mining**
- Fill in skeletal or **incomplete specifications** about a domain
- Complex AI systems cannot be completely derived by hand and require **dynamic updating** to incorporate **new information**. Learning new characteristics expands the expertise and lessens the weak-point of the system

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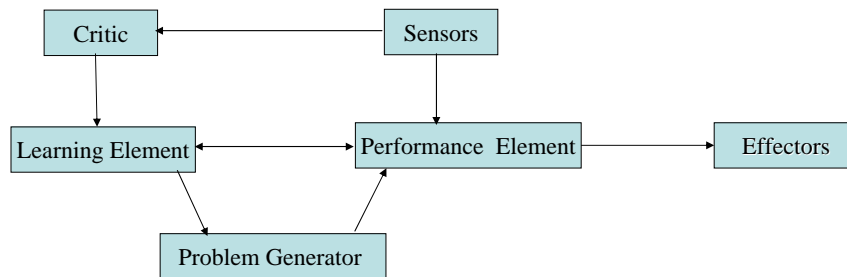
## Machine learning

- Application of Machine learning can be achieved by grouping those are **acquainted with existing machine learning methods** and **with the expertise in the given application domain to provide training data**



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## Components of a Learning System



- Learning Element **makes changes** to the system based on **how it's doing**
- **Performance Element** is the **agent** itself that acts in the world
- **Critic** tells the **Learning Element** how it is doing (e.g., success or failure) by comparing with a **fixed standard of performance**
- Problem Generator suggests "problems" or actions that will **generate new examples or experiences** that will aid in training the system

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## Evaluating learning algorithm Performance

Several possible criteria for evaluating a learning algorithm:

- Predictive **accuracy of classifier**
- Speed of **learner**
- Speed of **classifier**

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## Problem solving by computer

- In expert system, programming has been replaced by **knowledge-encoding**
- Machine learning knowledge encoding is supposed to be replaced by **induction from examples (training data)**
- The learning system aims at determining a description of a **given concept** from a set of **concept examples** provided by the **teacher** and from the **background knowledge**

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## Problem solving by computer

- Background knowledge contains the information about the language used to describe the **examples** and **concepts**
- A task is to be solved by a computer is how to **translate the problem into computational items**
- In machine learning, this means how to represent **concepts, examples**, and the **background knowledge** → by some **representation languages**

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## Problem solving by computer

- The learning system should be able to deal with **imperfections of data** → examples will often contain a certain amount of **noise – errors** in the **descriptions** or in the **classifications**
- Examples can be **incomplete** in the sense that **some attribute values are missing** → **background knowledge** need not be **perfect**

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## Learning algorithm

Classified into two major categories:

- **Black-box method** such as neural network or mathematical statistical
  - Develop their own concept representation that is to be used for **concept recognition** purpose
  - Typically involves numerical calculation of **coefficients, distances or weights**
- **Knowledge-oriented method** aims at creating **symbolic knowledge structures** that satisfy the principle of **comprehensibility**.

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## Distinction criteria of concept learning

- Weak criterion → the system uses **sample data** to generate an **updated basis** for **improved performance** on subsequence data
- Strong criterion → weak criterion is satisfied and the system can communicate its **internal updates** in explicit **symbolic form**
- Ultra-strong → both weak and strong criteria are satisfied and the system can communicate its internal updates in an **operationally effective symbolic form**

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## Distinction criteria of concept learning

- **Artificial neural networks** and **statistical methods** satisfies the **weak criterion**
- **Artificial intelligence researcher** have been concerned with the **strong criterion**
- This book is concerned with the **knowledge-oriented algorithms** capable of developing **descriptions** understandable to the user.
- Most of these methods are based on manipulating **symbolic structures** for machine learning to form a **concept**

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## Cognitive perspective

- Even when concepts can be defined precisely, a **correct classification** of an object based on the available data may present a difficult problem
- By a **cluster**, statisticians mean a **group of objects** that are relatively close to each other according to a chosen **numerical distance**
- **Group of related concepts** can often be organized into a **generalization hierarchy** represented by a tree or graph

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## Cognitive perspective

- Three important notions are suitable to the **mutual relations** among **concept brief exposition: basic-level effect, typicality, and contextual dependency**
- In an **ordered hierarchy** of concepts, one level can be understood as **basic**.
- The basic means that the concept on this level **shares with sub-concepts** a large number of **features** that can be described in **recognizable terms**

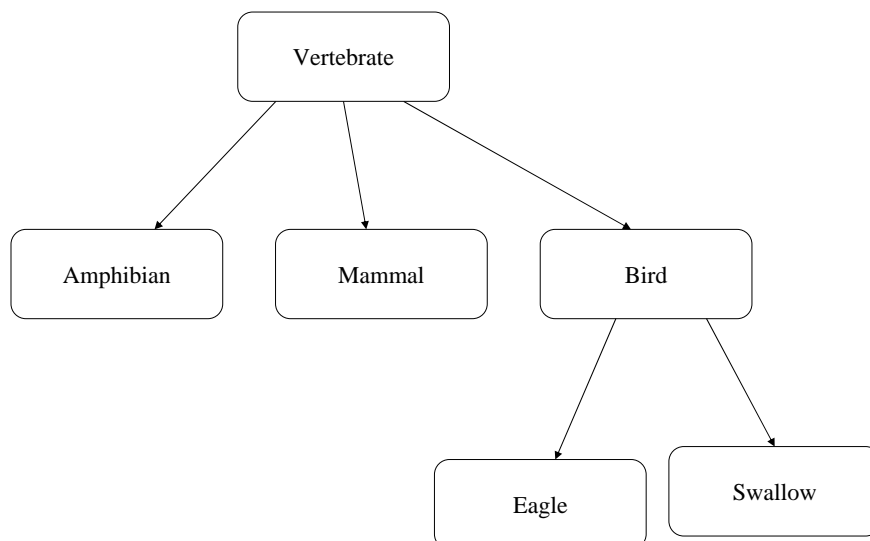
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## Cognitive perspective

- Eagle → bird (**basic-level concept:wings,beak**)  
→ animal ?→ living being (not basic)
- BMW → car (basic-level concept) →  
transportation
- The concepts on **lower levels** can be  
understood as **specializations** of the **basic-level  
concepts**, whereas concepts on higher levels  
are often defined as **groups of basic-level  
concepts** sharing some important **feature**

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## Symbolic form



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## Cognitive perspective

- **Typicality of distance** plays a crucial role for learning a given concept
- Measure **typicality** by the number of features **shared with other sub-concepts** and by the number of features **inherited from super-concepts** (the greater number of inherited features can be found in the instance, the more typical the instance is)
- Real-world concepts are learnable only in an appropriate context (**context dependency** measurement)

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## Cognitive perspective

- A task to be solved by computer is how to **translate the problem into computation terms**
- How to represent concepts, examples, and the background knowledge by **representation language**
- Representation languages include Zero-order logic, attribute-value logic, Horn clauses, and second-order logic

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## Zero order logic

- Propositional calculus
- **Examples and concepts** are described by conjunction of Boolean constants that stand for **individual features (attribute values)**

$c \Leftarrow x \wedge y \wedge z$  ( an object is an instance of the concept  $c$  whenever the conditions  $x, y, z$  hold simultaneously)

$\text{can\_marry\_jane} \Leftarrow \text{male} \wedge \text{grown\_up} \wedge \text{single}$

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## Zero order logic

- It describes only **simple concepts** and is difficult to capture **complex concepts** encountered in daily life
- It has **low descriptive power** and **excluded widespread application of zero order logic** in machine learning
- Can only be used to illustrate simple algorithms

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## Attributional Logic

- It improves over the zero-order logic is that the **attributes** are **variables** that can take on various values.
- \* stands for any one, the **or** linking two or more attribute values is called **internal disjunction**
- **Examples** are presented in a **table**, each row represents **an example** and each column stands for an **attribute** ( $c \Leftarrow x \wedge y \wedge z$ )
- How a car can attract for a young entrepreneur?

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## Can table analysis

| Object | Make     | Size   | Price      | Classification |
|--------|----------|--------|------------|----------------|
| Car1   | European | Big    | Affordable | ⊕ (positive)   |
| Car2   | Japanese | Big    | Affordable | ⊕              |
| Car3   | European | Medium | Affordable | ⊗ (negative)   |
| Car4   | European | Small  | Affordable | ⊗              |
| Car5   | European | Medium | Expensive  | ⊕              |
| Car6   | Japanese | Medium | Affordable | ⊗              |
| Car7   | Japanese | Medium | Expensive  | ⊕              |
| Car8   | European | Big    | Expensive  | ⊕              |

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## Attributional Logic

- **Boolean, numeric, symbolic, or mixed-value attributes** can be considered, **the scope of their value** is often **constrained** by background knowledge
- Attributional logic (**variable-value logic**) is more practical than zero-order logic and provided the **basis** for machine learning algorithms (TDIDT '86 or AQ '83)
- A formal basis for such a description language was defined in **variable-valued logic**

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## First Order predicate Logic definition

FOL (Horn clause) supplies these primitives:

- **Variable symbols.** E.g.,  $x, y$
- **Connectives.** Same as in PL: not ( $\sim$ ), and ( $\wedge$ ), or ( $\vee$ ), implies ( $\Rightarrow$ ), if and only if ( $\Leftrightarrow$ )

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## FOL definition

- **Quantifiers:** Universal ( $\forall$ ) and Existential ( $\exists$ )
  - **Universal quantification** corresponds to conjunction in that  $(\forall x)P(x)$  means that **P holds for all values of x in the domain associated with that variable**. E.g.,  $(\forall x)$  dolphin(x)  $\Rightarrow$  mammal(x)
  - **Universal quantifiers** usually used with "implies" to form "if-then rules." E.g.,  $(\forall x)$  IE-student(x)  $\Rightarrow$  smart(x) means "All IE students are smart." You can use universal quantification to make blanket statements about every individual in the world:  $(\forall x)$ IE-student(x)  $\wedge$  smart(x) meaning that **everyone in the world is a IE student and is smart**.

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## FOL definition

- Existential quantifiers usually used with "and" to specify **a list of properties or facts about an individual**.
  - E.g.,  $(\exists x)$  IE-student(x)  $\wedge$  smart(x) means "there is a IE student who is smart." A common mistake is to represent this English sentence as the FOL sentence:  $(\exists x)$  IE-student(x)  $\Rightarrow$  smart(x). But consider what happens when there is a person who is NOT a IE-student.
  - **Existential quantification** corresponds to disjunction in that  $(\exists x)P(x)$  means that **P holds for some value of x in the domain associated with that variable**. E.g.,  $(\exists x)$  mammal(x)  $\wedge$  lays-eggs(x)

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## FOL definition

- Switching the order of **universal quantifiers does not change the meaning**:  $(\forall x)(\forall y) P(x,y)$  is logically equivalent to  $(\forall y)(\forall x) P(x,y)$ . Similarly, you can **switch the order of existential quantifiers**.
- Switching the order of **universals and existentials does change meaning**:
  - **Everyone likes someone**:  $(\forall x)(\exists y) \text{likes}(x,y)$
  - **Someone is liked by everyone**:  $(\exists y)(\forall x) \text{likes}(x,y)$

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Sentences are built up from terms and atoms

- A **term** (denoting a **real-world individual**) is a constant symbol, a variable symbol, or an **n-place function of n terms**. For example,  $x$  and  $f(x_1, \dots, x_n)$  are terms, where each  $x_i$  is a term.
- An **atom** (which has value **true or false**) is either an **n-place predicate of n terms**, or, **if P and Q are atoms**, then  $\sim P$ ,  $P \vee Q$ ,  $P \wedge Q$ ,  $P \Rightarrow Q$ ,  $P \Leftrightarrow Q$  are atoms

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Sentences are built up from terms and atoms

- A **sentence** is an **atom**, or, if **P** is a **sentence** and **x** is a **variable**, then  $(\forall x)P$  and  $(\exists x)P$  are sentences
- A **well-formed formula (wff)** is a sentence **containing no "free" variables**. i.e., **all variables are "bound" by universal or existential quantifiers**. E.g.,  $(\forall x)P(x,y)$  has  $x$  bound as a universally quantified variable, but  $y$  is free.

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## Translating English to FOL

- Every gardener likes the sun.  
 $(\forall x) \text{gardener}(x) \Rightarrow \text{likes}(x, \text{Sun})$
- You can fool **some of the people all of the time**.  
 $(\exists x)(\forall t) (\text{person}(x) \wedge \text{time}(t)) \Rightarrow \text{can-fool}(x,t)$
- You can fool **all of the people some of the time**.  
 $(\forall x)(\exists t) (\text{person}(x) \wedge \text{time}(t) \Rightarrow \text{can-fool}(x,t)$
- All purple mushrooms are poisonous.  
 $(\forall x) (\text{mushroom}(x) \wedge \text{purple}(x)) \Rightarrow \text{poisonous}(x)$

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## Translating English to FOL

- No purple mushroom is poisonous.  
 $\sim(\exists x) \text{purple}(x) \wedge \text{mushroom}(x) \wedge \text{poisonous}(x)$   
or, equivalently,  
 $(\forall x) (\text{mushroom}(x) \wedge \text{purple}(x)) \Rightarrow$   
 $\sim\text{poisonous}(x)$
- There are exactly **two purple mushrooms**.  
 $(\exists x)(\exists y) \text{mushroom}(x) \wedge \text{purple}(x) \wedge$   
 $\text{mushroom}(y) \wedge \text{purple}(y) \wedge \sim(x=y) \wedge (\forall z)$   
 $(\text{mushroom}(z) \wedge \text{purple}(z)) \Rightarrow ((x=z) \vee (y=z))$

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## Translating English to FOL

- Deb is not tall.  
 $\sim\text{tall}(\text{Deb})$
- X is above Y if X is on directly on top of Y or  
else there is a pile of one or more other objects  
directly **on top of one another starting with X** and  
**ending with Y**.  
 $(\forall x)(\forall y) \text{above}(x,y) \Leftrightarrow (\text{on}(x,y) \vee (\exists z)$   
 $(\text{on}(x,z) \wedge \text{above}(z,y)))$

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## First Order predicate Logic – Horn Clause

- Inference Rule -- A **Horn clause (FOL)** consists of a **head** and a **body** as illustrated by the following definition:

**grandparent(x,y) :- parent(x,z), parent(z,y)**

- The **left** part of :- is called the **head**, and the **right** part of :- is the **body**, the **commas** stands for conjunctions of **universal quantified**
- **Grandparent** and **parent** are called **predicate** and the **variables** in the parentheses are called **arguments**

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## First Order predicate Logic – Horn Clause

- If all **predicates** have precisely **one argument**, the language reduces into **attribute-value logic**
- If all **predicates** have precisely **zero argument**, the language reduces into **zero-order logic**
- Horn clauses constitute an advanced representation language that facilitates very complex description
- This form is the basis of a programming language  
→ **Prolog**

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## Second-Order Logic(SOL)

- Built on the idea of the **predicate name** can be considered as **variables**

$p(x,y) :- q(x,xw) \wedge q(y,yw) \wedge r(xw,yw)$

for examples

1.  $brothers(x,y) :- son(x,xw) \wedge son(y,yw) \wedge equal(xw,yw)$

$\Theta = \{p=brothers, q=son, r=equal\}$

2.  $lighter(x,y) :- weight(x,xw) \wedge weight(y,yw) \wedge less(xw,yw)$

$\Theta = \{p=lighter, q=weight, r=less\}$

→ **groups of concepts** share the same **structure** of admissible descriptions

→ SOL is successfully used such structures to assist the **search for the concept**

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## Explicit constrained languages

- Representation languages based on **logic** are so **rich and flexible** that their use for machine learning is **computational intractable**
- Some constraints such as **a limited number of predicates in the clause, a limited number of predicate arguments, excluded recursive definitions**

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## Explicit constrained languages

- The number of variables in the **body** of the clause is not allowed to **exceed a predefined threshold** (only those variables can appear in the body that have **already appeared in the head of the clause**)

`ancestor(x,y) :- parent(x,z), parent(z,y)` in FOL

`ancestor(x,y) :- parent(x,y)` should be added to  
avoid recursion

`ancestor(x,y) :- parent(x,z), ancestor(z,y)`

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